

How far removed are you?

Scalable Privacy-Preserving Estimation of Social Path Length with Social PaL

N. Asokan

joint work with Marcin Nagy, Thanh Bui, Emiliano De Cristofaro, Ahmad-Reza Sadeghi, Jörg Ott

Problem

How can you find if you have common friends with someone (nearby)?

... in a privacy-preserving way

Applications

- ◆ Intuitive means for specifying access control
 - ◆ Ride sharing
 - ◆ Tethering Internet access
 - ◆ ...
- ◆ Information
 - ◆ Friend radar
- ◆ ...

Requirements

◆ **privacy:**

- ◆ no more info. to participants than about common friends
- ◆ no additional info. to anybody else (e.g., “trusted server”)

◆ **authenticity:**

- ◆ no false claims of friendship

◆ **efficiency:**

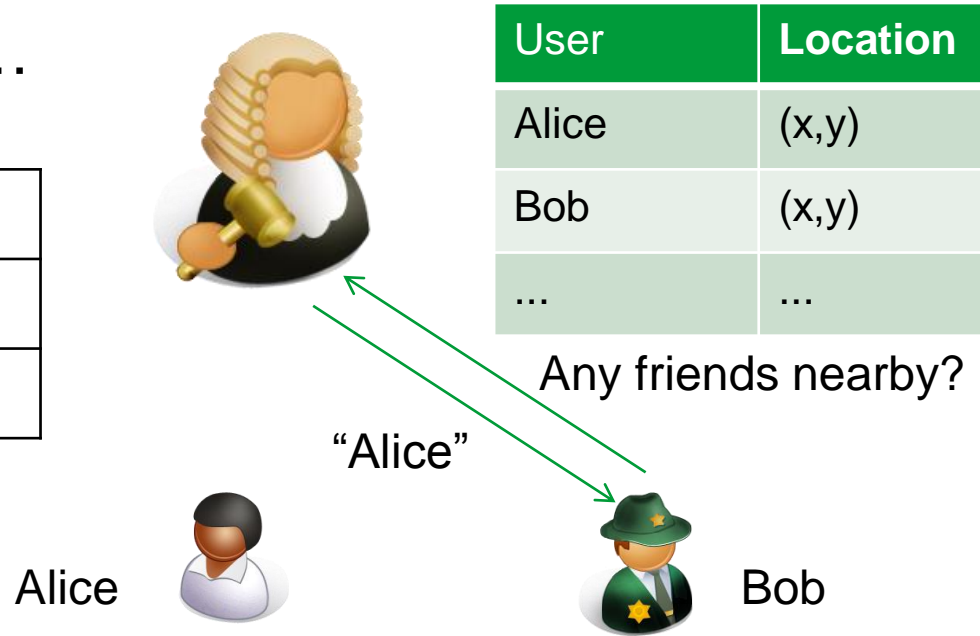
- ◆ applicable for mobile usage
- ◆ minimize expensive crypto operations

Current approach: Using a trusted server

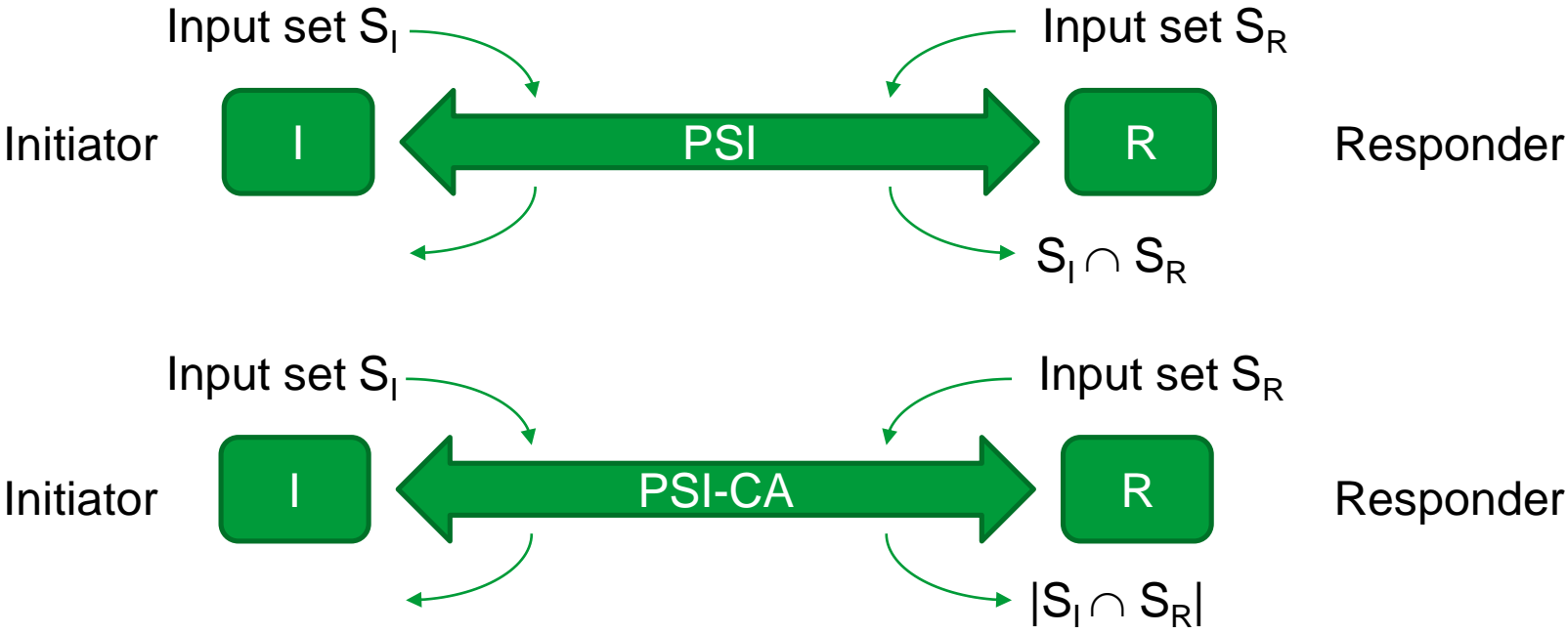
- ◆ FourSquare, Tencent, ...



Privacy	✗
Authenticity	✓
Efficiency	✓



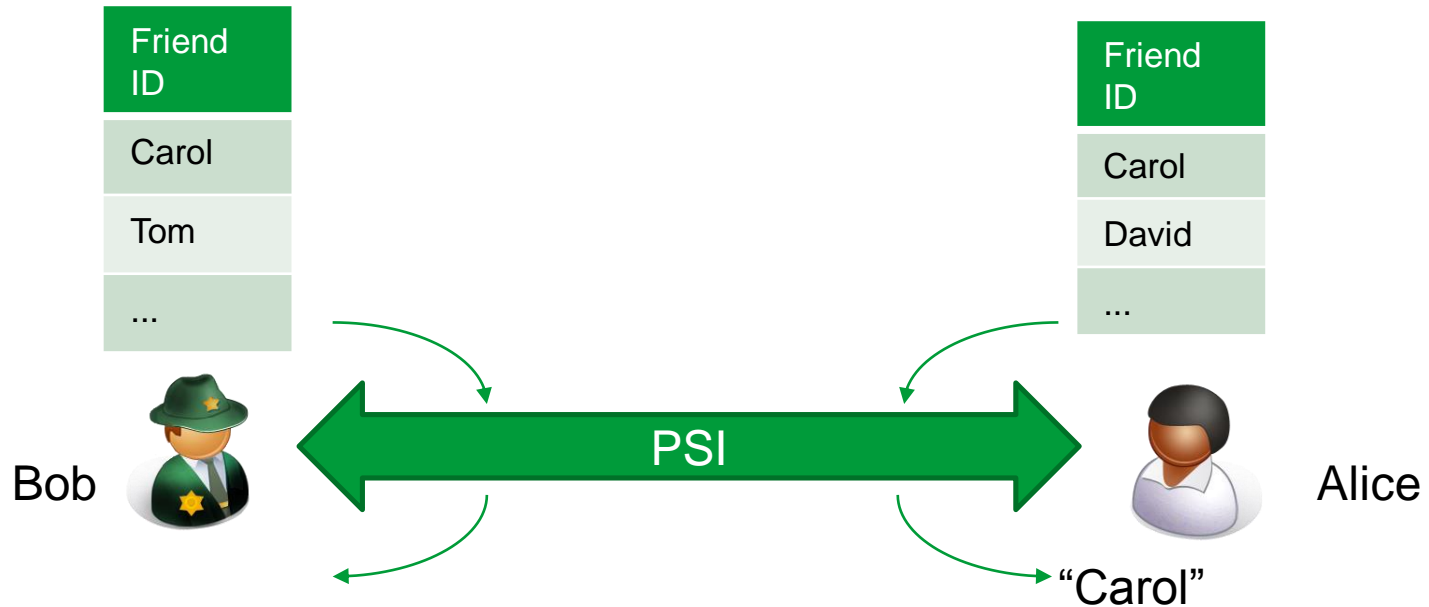
Alternative: Private Set Intersection Protocols



Secure in the honest-but-curious model
 $O(|S_I| + |S_R|)$ modular exponentiations

[De Cristofaro et al, [FC'10](#), [Asiacrypt '10](#), [CANS'12](#)]

Finding Common Friends using PSI naively



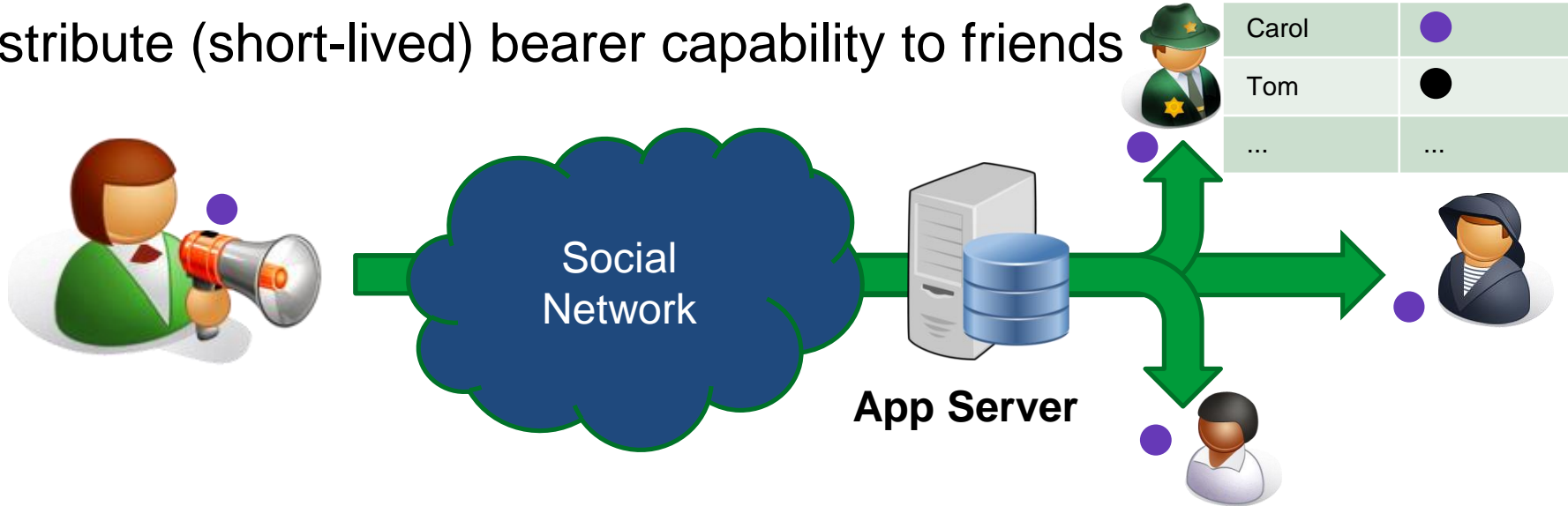
Privacy	?
Authenticity	×
Efficiency	×

Approach

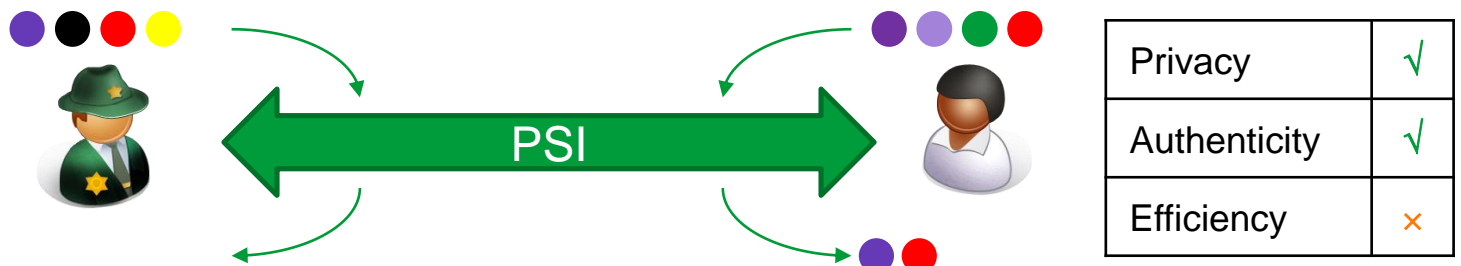
- Make use of widely deployed online social networks
 - user authentication, social graph
- But don't cede even more information to them

Finding Common Friends using PSI with capabilities

1. Distribute (short-lived) bearer capability to friends



2. Private Set Intersection on capability sets to find common friends

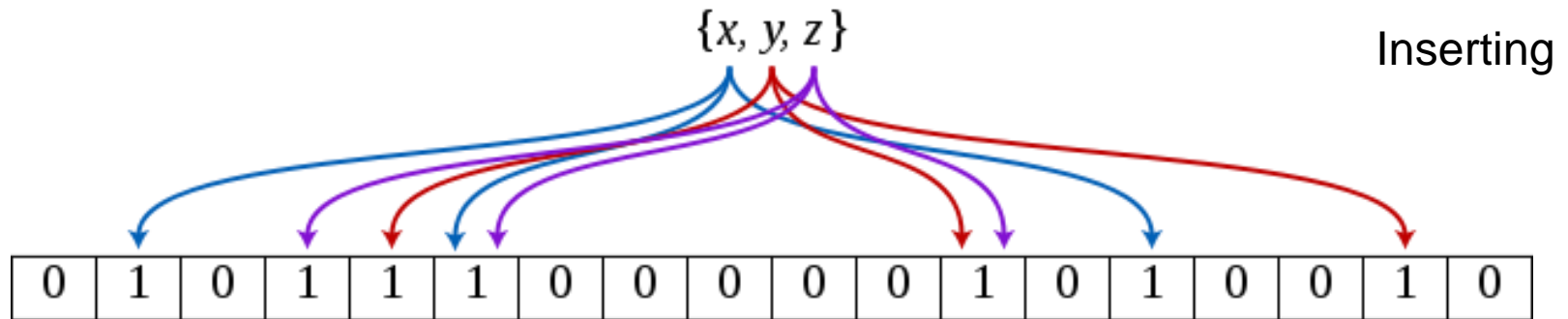


Can we build a fast “PSI”?

- Why are classic PSIs slow?
 - ◆ Designed to work even when input sets are enumerable
 - ◆ i.e., elements are predictable
 - ◆ Naive hash-each-element approach fast, but insecure for enumerable input sets
 - ◆ However, bearer capabilities are random
 - ◆ Hash-each-element approach is safe
 - ◆ Still $O(n)$ communication complexity
 - ◆ **Idea: use a Bloom Filter to represent input set**
-

What is a Bloom Filter?

Efficient data structure for testing set membership
Map each element to k positions in a bit vector



No false negatives; false positives possible

Source: Wikipedia

Bloom Filter PSI Protocol

Initiator I

Responder R

Challenges
● ● ● ●

Insecure channel

Man-in-the-middle

False positives

Secure channel establishment

Channel binding

insert elements into BF → *BF* → *check each element for presence in BF*

False positives removal e.g., challenge-response

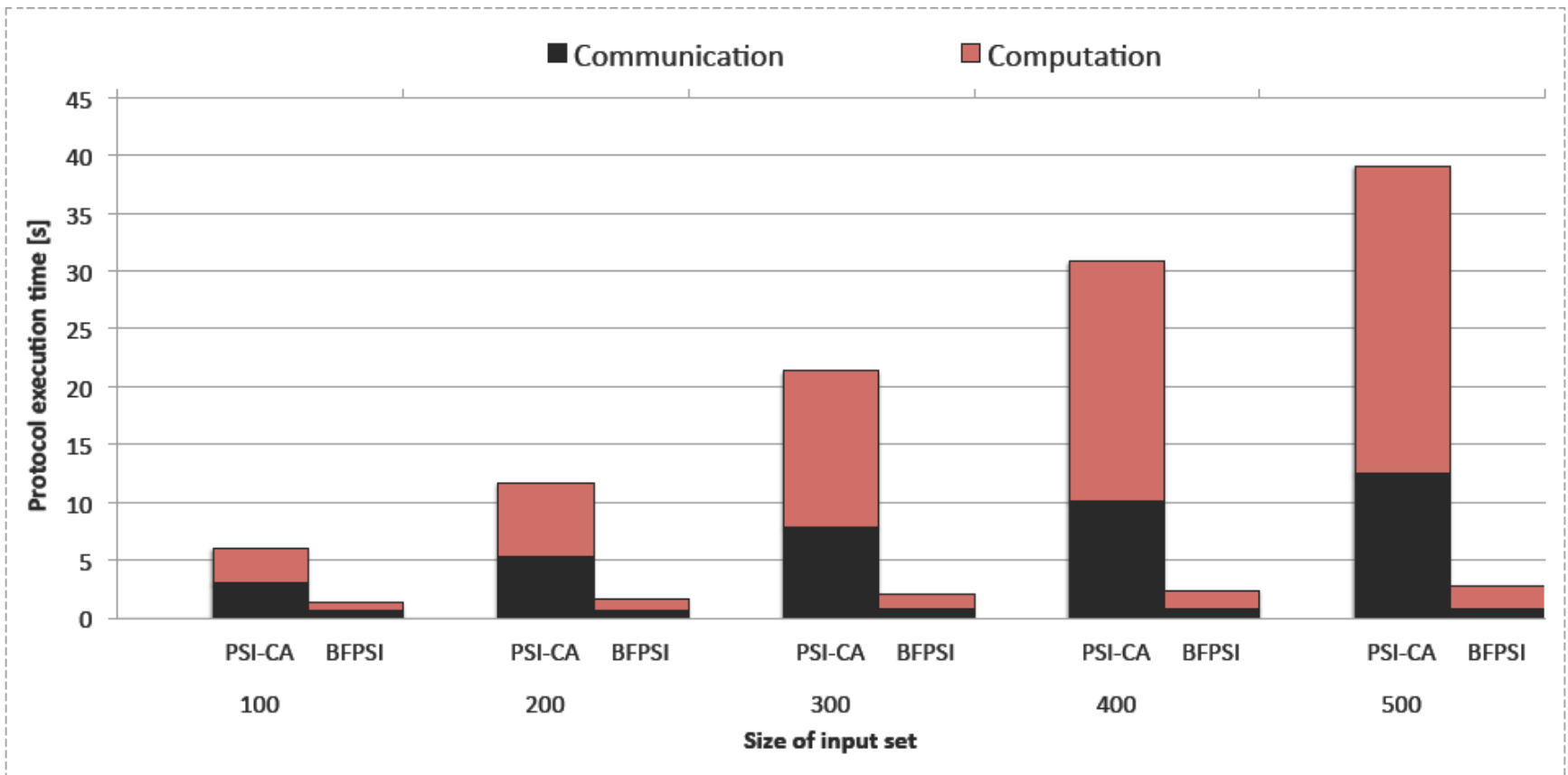
● ● ● ●

Privacy	✓
Authenticity	✓
Efficiency	✓

Not a replacement for PSI in general!

● ●

Comparison: execution time



Two challenges with Common Friends

- Bootstrapping is a problem
- Limited to social paths of length 2

Bootstrapping the system

- Only participating users upload capabilities



The system can **only find common friends who are participating in the system**

Fixing bootstrapping: Ersatz profiles

Assumption:

1. App server may query Social Network for list of friends of a participating user

Have App server create replacements for missing profiles

1. Identify friends of participating users
2. Create/maintain capabilities for those missing

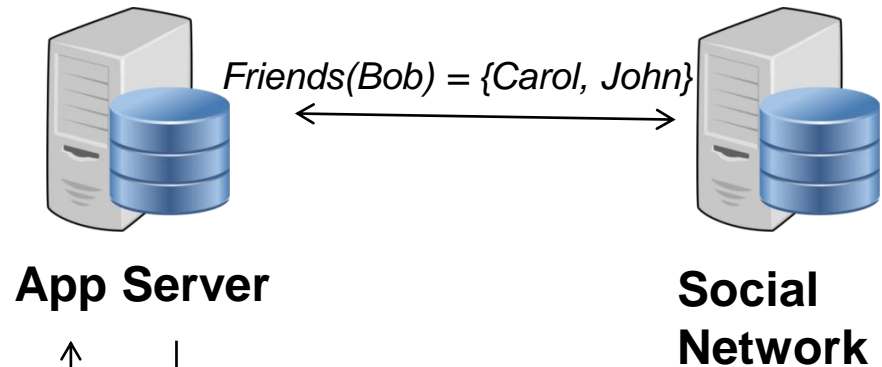
Ersatz profile = Social Network identity + server generated capability

Fixing bootstrapping: Ersatz profiles

(3) Server generates ersatz profiles for missing users

User	Capability
Carol	●
Bob	●
John	●

(2) Server retrieves Bob's friends



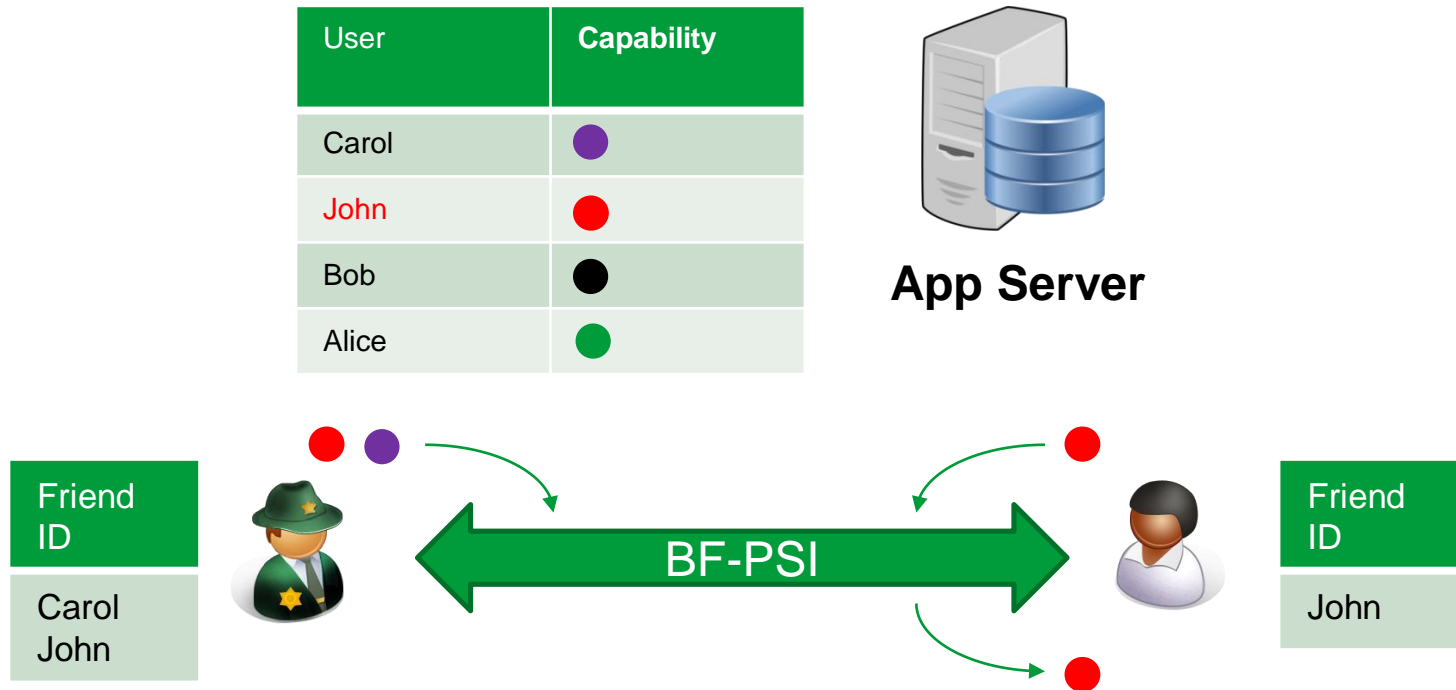
(1) Bob uploads capability
 $(Bob, \text{black dot})$

(4) Bob downloads capabilities

$(Carol, \text{purple dot})$
 $(John, \text{red dot})$



Fixing bootstrapping: Ersatz profiles



With **ersatz profiles** all common friends are **always** discovered

Finding lengths of longer social paths

How can you find your social graph “distance” to someone (nearby)?

... in a privacy-preserving way

Social PaL: Social Path Length Finder

More applications

- ◆ Intuitive means for specifying access control
 - ◆ Ride sharing
 - ◆ Tethering Internet access
 - ◆ ...
- ◆ Information
 - ◆ Friend radar
- ◆ Routing in “dense” ad-hoc environment
- ◆ Place familiarity estimation
- ◆ ...

Social Path Length

Definition:

minimum number of hops in social graph
between two users

Additional requirements

◆ Privacy:

- ◆ Two users can't learn more than by gathering information using standard social network interfaces available to them

◆ Functional:

- ◆ Maximize number of paths discovered between two users
- ◆ Determine exact path length between two users

Capabilities as path length proofs

Intuition:

1. Capability distributed to friends used as friendship proof
2. Use hash chains to generate **higher order capabilities**

From capability c generate i^{th} order capability:

$$h^i(c) = c^i \quad \text{①}$$

1. Distribute c^i to contacts $i+1$ hops away
2. Recipient includes c^i, c^{i+1}, \dots, c^n in input to PSI

Social PaL graph building

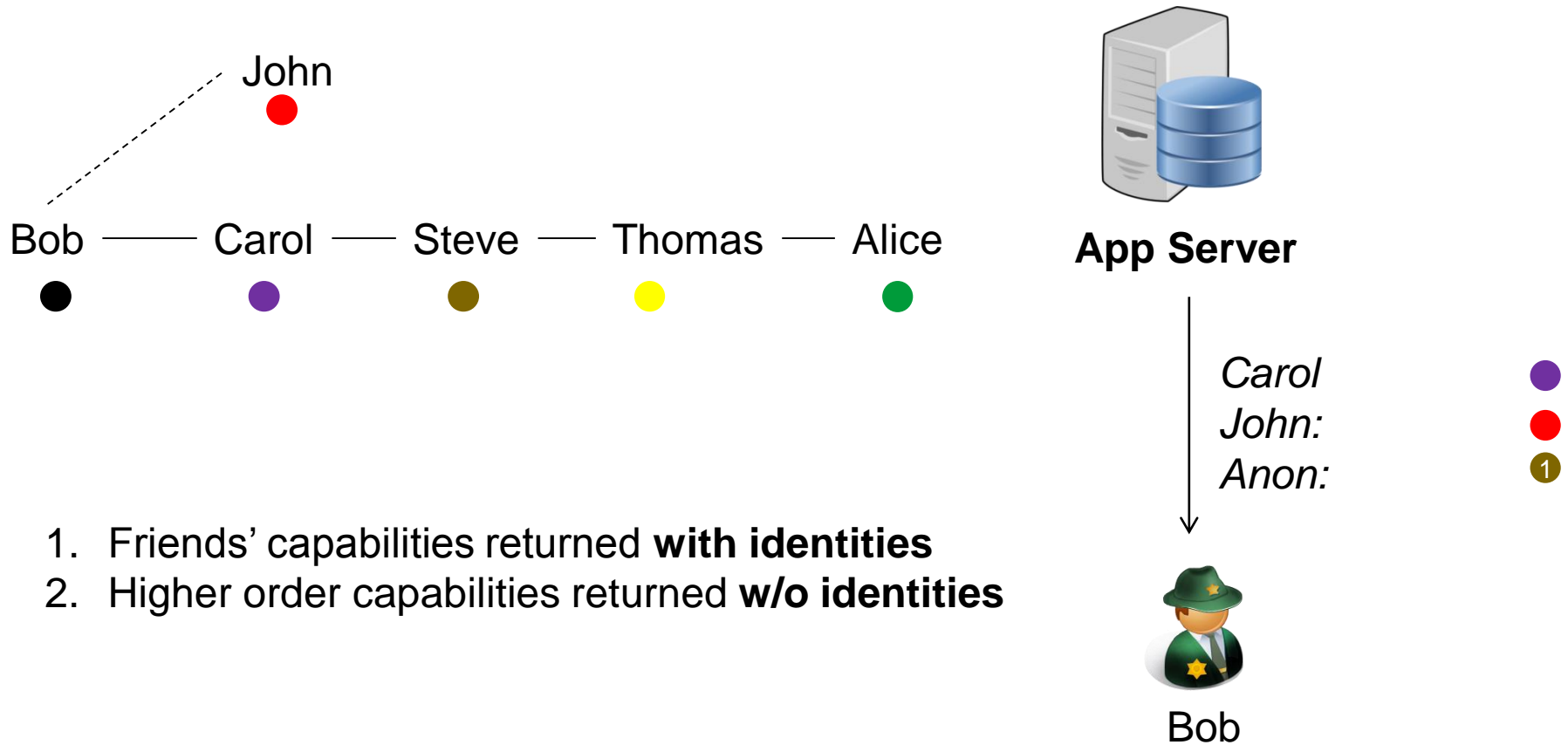
Social PaL only learns friend lists of actual users

- users explicitly authorize Social PaL

If relationships in the social network are reciprocal

- Partial view of friend lists of ersatz profiles possible

Social PaL capability distribution



1. Friends' capabilities returned **with identities**
2. Higher order capabilities returned **w/o identities**

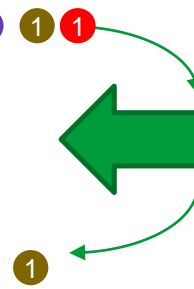
Social PaL path length discovery

Friend ID	
Carol	① ②
Anon	②
John	① ②

② + ② = 4



Bob



BF-PSI

$D(\text{Bob}, \text{Alice})=4$



Alice

② + ② = 4

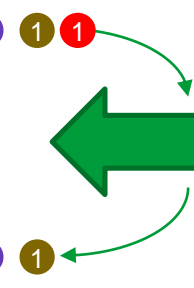
Friend ID	
Thomas	① ②
Anon	②

Friend ID	
Carol	① ②
Anon	②
John	① ②

② + ② = 4
① + ② = 3



Bob



BF-PSI

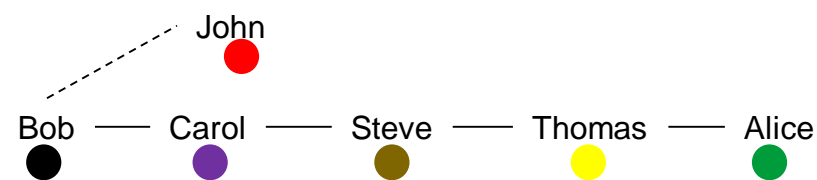
$D(\text{Bob}, \text{Thomas})=3$



Thomas

② + ② = 4
① + ② = 3

Friend ID	
Alice	① ②
Steve	① ②
Anon	①



Coverage of social path discovery

- *Theorem:* If Social PaL discovers a path between A and B, then both A and B can determine its **exact length**.
- **Coverage:** probability that A & B will discover a k-hop path that exists between them in the social network

Dataset for estimating coverage

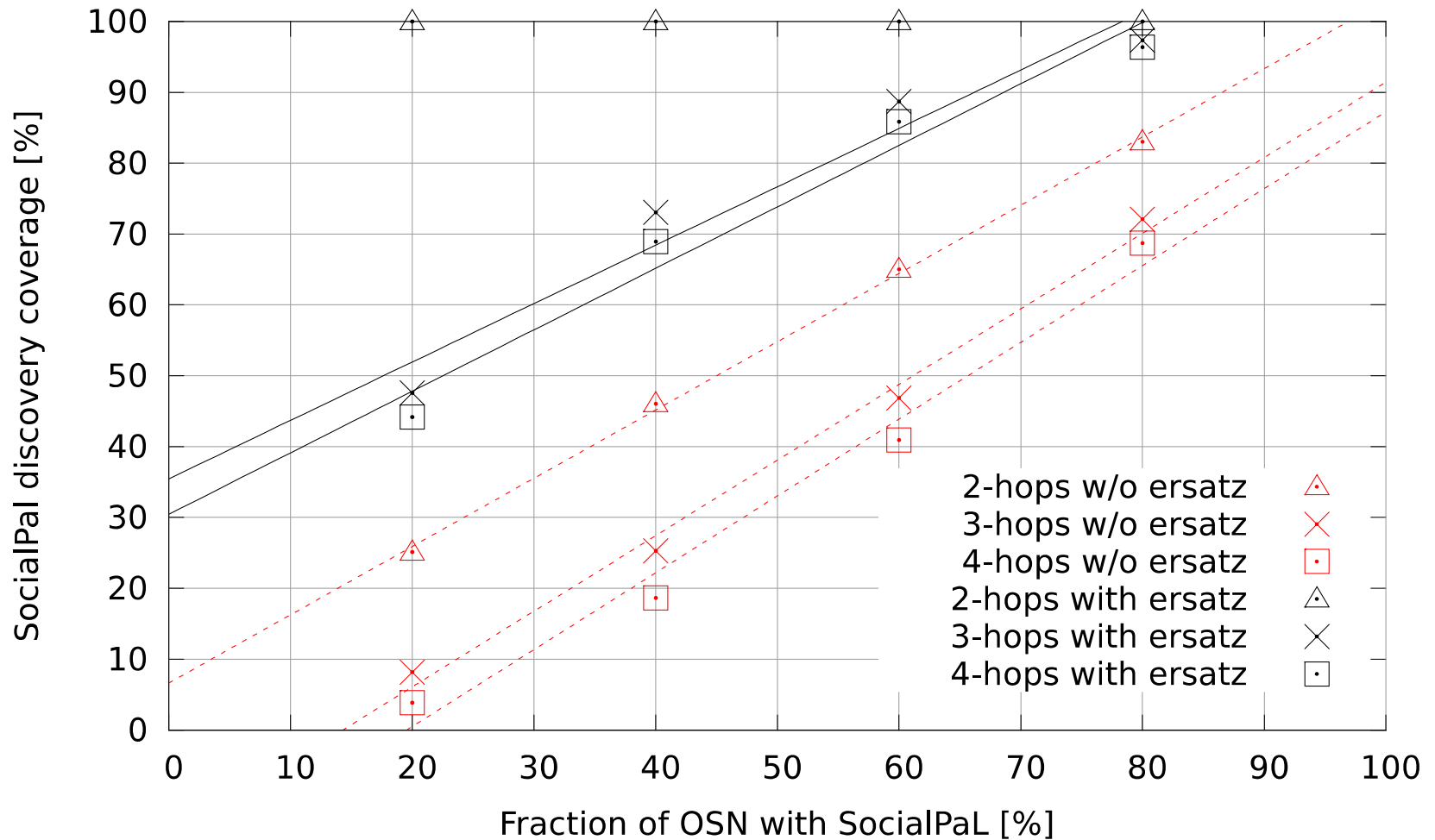
- Social Filter dataset
 - By Sirivanos et al
 - Derived from dataset by Gjoka et al (UC Irvine)
 - 500 000 users; 30 connections on average

Simulation for estimating coverage

1. Test set: randomly choose $x\%$ of users
 - $x = 20, 40, 60, 80$ (represents fraction using Social Pal)
2. Pick 50k pairs randomly from “test set” w/ k -hop path
 - $k = 2, 3, 4$
3. Compute fraction for which Social PaL discovers path

Repeat steps 1-3 ten times; average results

Coverage: Social Filter dataset



Datasets for estimating coverage

- Social Filter dataset
 - By Sirivanos et al
 - Derived from dataset by Gjoka et al (UC Irvine)
 - 500 000 users; 30 connections on average
 - Sampling did not preserve node degree

Dataset for estimating coverage

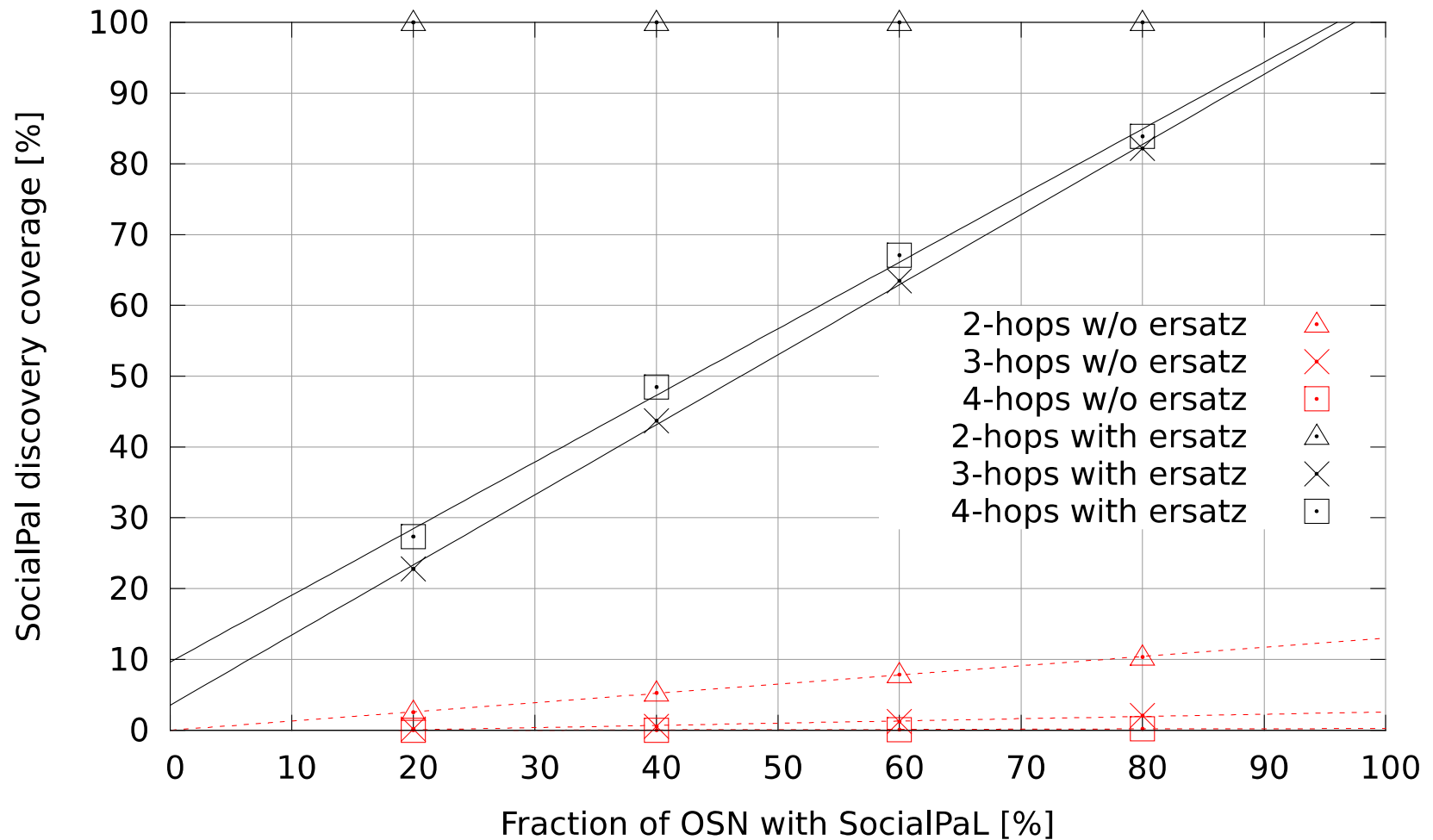
- MHRW dataset
 - Sampled using Metropolis Hastings random walk
 - 95 700 “sampled users”, 175 connections on average
 - 72.2 million “outside users”
 - among sampled users: 3 connections on average
- From Gjoka et al (Infocom 2010)

Simulation for estimating coverage

1. Test set: randomly choose $x\%$ of “sampled users”
 - $x = 20, 40, 60, 80$ (represents fraction using Social Pal)
2. Pick 50k pairs randomly from “test set” w/ k -hop path
 - $k = 2, 3, 4$
3. Compute fraction for which Social PaL discovers path

Repeat steps 1-3 ten times; average results

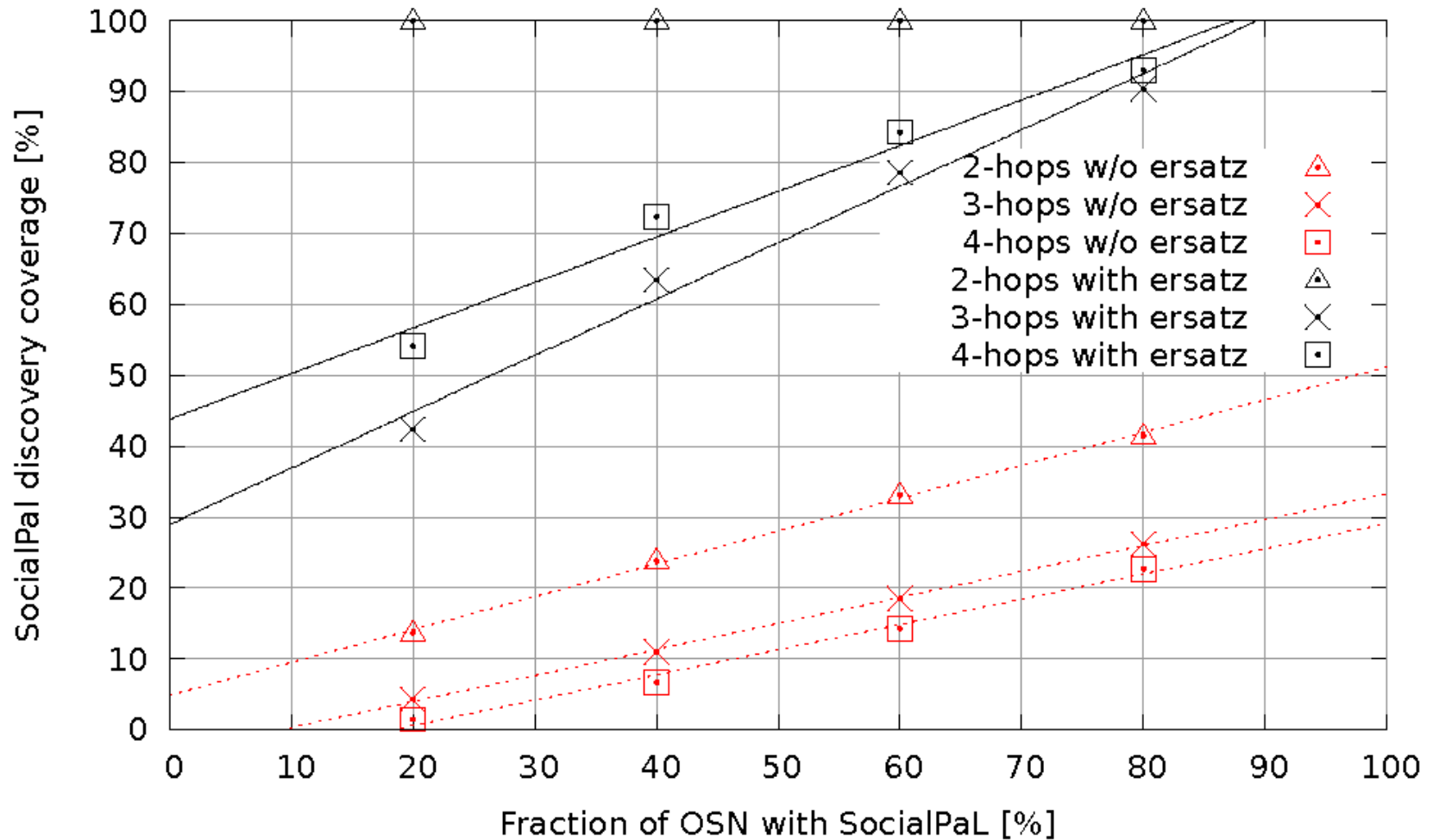
Coverage: MHRW dataset (random walk)



Dataset for estimating coverage

- BFS dataset
 - Sampled using breadth-first search
 - 2.2 million sampled users, 310 connections on average
 - among sampled users: 53 connections on average
- Also from Gjoka et al (Infocom 2010)

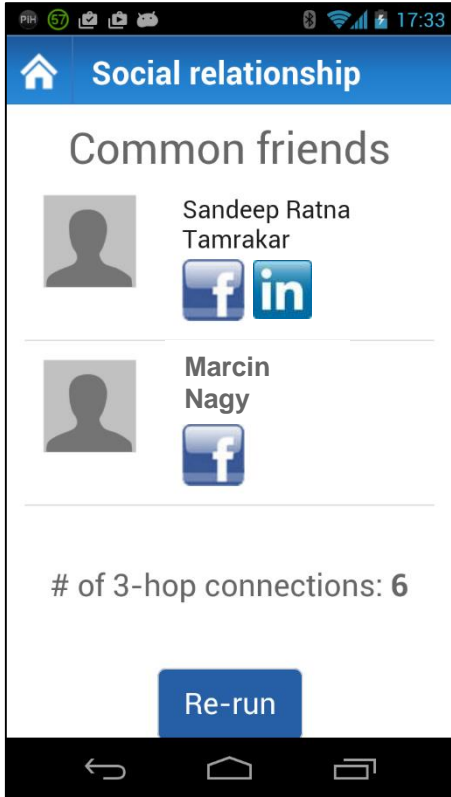
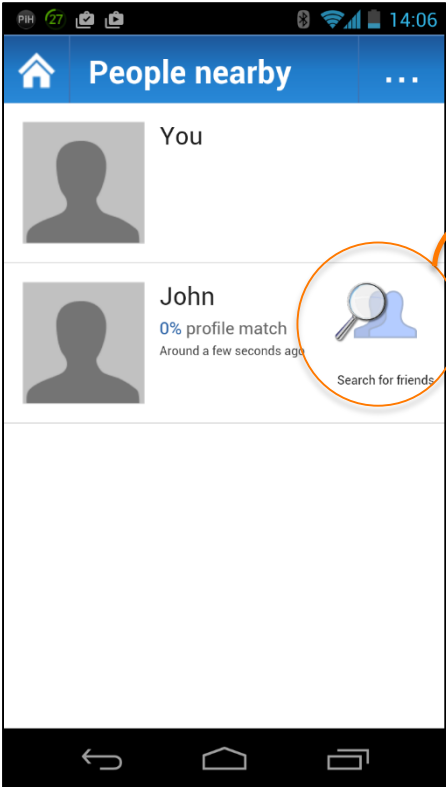
Coverage: Breadth-first search dataset



Coverage analysis summary

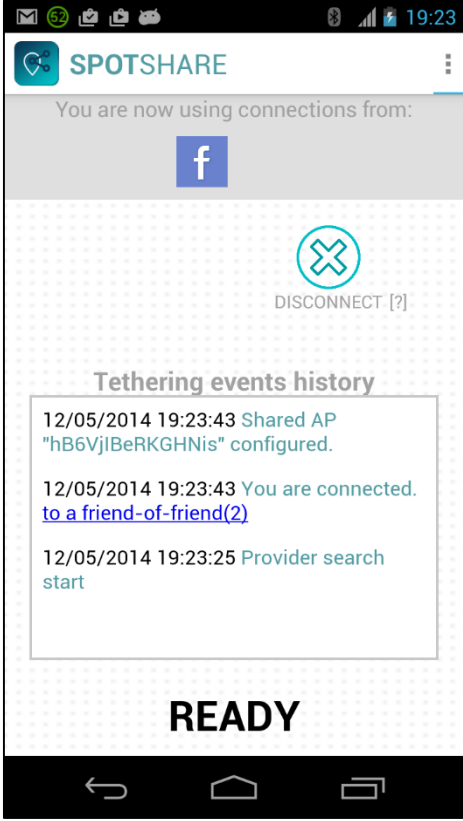
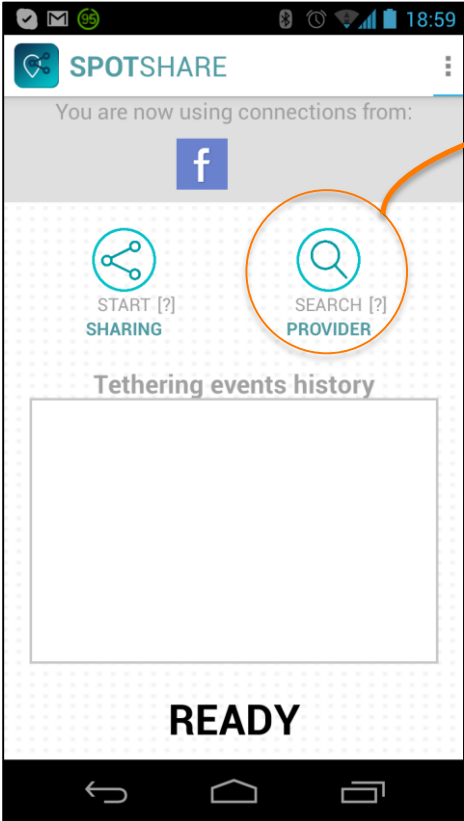
- Use of ersatz profiles significantly increases coverage
 - Always 100 % coverage for 2-hop paths (detects all)
 - Only 20% users with Social PaL: coverage > 40%
 - Except for MHRW dataset
 - 80% users with Social PaL: coverage > 80%, always
- Coverage is better in datasets with higher connectivity
 - BFS dataset ~ Social Network in regions with high penetration
- 4-hop paths more readily discovered than 3-hop paths!

Example App: nearbyPeople



[nearbyPeople](#)

Example App: SpotShare



[SpotShare](#)
(Google Play)

Summary

- Privacy-preserving, scalable protocols for finding
 - common friends
 - lengths of social paths
- Used in two applications (available for download)
 - Easy-to-use tethering (“SpotShare”)
 - Friend radar (“nearbyPeople”)
- Source code available for research use
- More info at <https://se-sy.org/projects/pet/>

